

$$25-7. \text{ (a) } \delta_{A1} = \left(\frac{2}{\sigma \mu_0 \omega} \right)^{1/2} = \left(\frac{2}{3.54 \times 10^7 (4\pi \times 10^{-7}) 2\pi \times 6 \times 10^4} \right)^{1/2} \text{ m} = 0.345 \text{ mm}$$

$$\text{(b) } \delta_{s.w.} = \left(\frac{3.54 \times 10^7}{4.3} \right) \times \delta_{A1} = 0.991 \text{ m} \approx 1 \text{ m}$$

$$25-8. \delta_{Ag} = \left(\frac{\lambda}{\sigma \mu_0 \pi c} \right)^{1/2} = \left(\frac{0.1}{3 \times 10^7 (4\pi \times 10^{-7}) \pi (3 \times 10^8)} \right)^{1/2} \text{ m} = 1.68 \times 10^{-6} \text{ m} = 1.68 \mu\text{m}$$

As long as the silver coating is thicker than this the silver-plated brass component would work.

$$25-9. \text{ (a) } I = I_0 e^{-\alpha x} \Rightarrow (I/I_0) = (1/4) = e^{-\alpha x} = e^{-\alpha(3.42\text{m})} \Rightarrow 3.42 \alpha = \ln(4) \Rightarrow \alpha = 0.405 \text{ m}^{-1}$$

$$\text{(b) } (I/I_0) = (1/100) = e^{-(0.405 \text{ m}^{-1})x} \Rightarrow (0.405 \text{ m}^{-1})x = \ln(100) \Rightarrow x = 11.37 \text{ m}$$

$$14-2. \text{ In general } \tilde{\mathbf{E}} = [E_{0x} e^{i\varphi_x} \hat{\mathbf{x}} + E_{0y} e^{i\varphi_y} \hat{\mathbf{y}}] e^{i(kz - \omega t)} = \begin{bmatrix} E_{0x} e^{i\varphi_x} \\ E_{0y} e^{i\varphi_y} \end{bmatrix} e^{i(kz - \omega t)} = \tilde{\mathbf{E}}_0$$

$$\text{(a) } \tilde{\mathbf{E}} = [E_0 \hat{\mathbf{x}} - E_0 \hat{\mathbf{y}}] e^{i(kz - \omega t)} \Rightarrow \tilde{\mathbf{E}}_0 = E_0 \begin{bmatrix} 1 \\ -1 \end{bmatrix} \Rightarrow \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}. \text{ Linearly polarized at } -45^\circ.$$

$$\text{(b) } \tilde{\mathbf{E}} = [E_0 \hat{\mathbf{x}} + E_0 \hat{\mathbf{y}}] e^{i(kz - \omega t)} \Rightarrow \tilde{\mathbf{E}}_0 = E_0 \begin{bmatrix} 1 \\ 1 \end{bmatrix} \Rightarrow \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}. \text{ Linearly polarized at } 45^\circ.$$

$$\text{(c) } \tilde{\mathbf{E}} = [E_0 \hat{\mathbf{x}} + E_0 e^{-i\pi/4} \hat{\mathbf{y}}] e^{i(kz - \omega t)} \Rightarrow \tilde{\mathbf{E}}_0 = E_0 \begin{bmatrix} 1 \\ e^{-i\pi/4} \end{bmatrix} \Rightarrow \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ \frac{1}{\sqrt{2}}(1 - i) \end{bmatrix}. \text{ Then,}$$

$$\tan 2\alpha = \frac{2E_{0x}E_{0y}\cos\epsilon}{E_{0x}^2 - E_{0y}^2} \rightarrow \infty \Rightarrow 2\alpha = 90^\circ, \alpha = 45^\circ$$

Right elliptically polarized at 45° .

$$\text{(d) } \tilde{\mathbf{E}} = [E_0 \hat{\mathbf{x}} + E_0 e^{i\pi/2} \hat{\mathbf{y}}] e^{i(kz - \omega t)} \Rightarrow \tilde{\mathbf{E}}_0 = E_0 \begin{bmatrix} 1 \\ e^{i\pi/2} \end{bmatrix} \Rightarrow \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ i \end{bmatrix}. \text{ Left-circularly polarized.}$$

$$14-3. \text{ In general } \tilde{\mathbf{E}} = [E_{0x} e^{i\varphi_x} \hat{\mathbf{x}} + E_{0y} e^{i\varphi_y} \hat{\mathbf{y}}] e^{i(kz - \omega t)} = \begin{bmatrix} E_{0x} e^{i\varphi_x} \\ E_{0y} e^{i\varphi_y} \end{bmatrix} e^{i(kz - \omega t)} = \tilde{\mathbf{E}}_0 e^{i(kz - \omega t)}$$

$$\text{(a) } \tilde{\mathbf{E}} = (2E_0 \hat{\mathbf{x}} + 0\hat{\mathbf{y}}) e^{i(kz - \omega t)} \Rightarrow \tilde{\mathbf{E}}_0 = 2E_0 \begin{bmatrix} 1 \\ 0 \end{bmatrix}. \text{ Linearly polarized along the } x\text{-direction. Velocity is in the } +z\text{-direction. The amplitude is } A = 2E_0 \sqrt{1^2 + 0^2} = 2E_0.$$

$$\text{(b) } \tilde{\mathbf{E}} = (3E_0 \hat{\mathbf{x}} + 4E_0 \hat{\mathbf{y}}) e^{i(kz - \omega t)} \Rightarrow \tilde{\mathbf{E}}_0 = E_0 \begin{bmatrix} 3 \\ 4 \end{bmatrix}. \text{ The polarization direction makes the angle } \alpha \text{ with the } x\text{-axis where,}$$

$$\alpha = \tan^{-1}(4/3) = 53^\circ$$

The wave is traveling in the $+z$ -direction with amplitude $A = \sqrt{3^2 + 4^2} E_0 = 5 E_0$.

$$\text{(c) } \tilde{\mathbf{E}} = 5E_0(\hat{\mathbf{x}} - i\hat{\mathbf{y}}) e^{i(kz + \omega t)} \Rightarrow \tilde{\mathbf{E}}_0 = 5E_0 \begin{bmatrix} 1 \\ -i \end{bmatrix}. \text{ The propagation is in the } +z\text{-direction. The wave is right-circularly polarized with amplitude. The electric field vector traces out a circle of radius } 5E_0.$$

14-4. (a) $\tilde{\mathbf{E}}_1 = E_{01}(\hat{\mathbf{x}} - \hat{\mathbf{y}})e^{i(kz - \omega t)} \Rightarrow \tilde{\mathbf{E}}_{01} = 2E_{01} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$. This is linearly polarized along -45°

$\tilde{\mathbf{E}}_2 = E_{02}(\sqrt{3}\hat{\mathbf{x}} + \hat{\mathbf{y}})e^{i(kz - \omega t)} \Rightarrow \tilde{\mathbf{E}}_{02} = E_{02} \begin{bmatrix} \sqrt{3} \\ 1 \end{bmatrix}$. This is linearly polarized along $\alpha = \tan^{-1}\left(\frac{1}{\sqrt{3}}\right) = 30^\circ$

The angle between the two is 75° .

(b) $\tilde{\mathbf{E}}_{01} \cdot \tilde{\mathbf{E}}_{02} = E_{01} E_{02}(\sqrt{3} - 1) = (\sqrt{2} E_{01})(\sqrt{3+1^2} E_{02}) \cos(\theta_{12}) \Rightarrow \cos \theta_{12} = \frac{\sqrt{3}-1}{2\sqrt{2}} \Rightarrow \theta_{12} = 75^\circ$