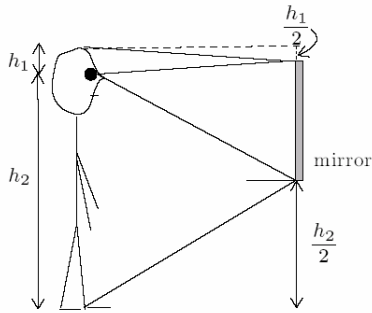


2-4. See the figure below. Let the height of the person be $h = h_1 + h_2$.

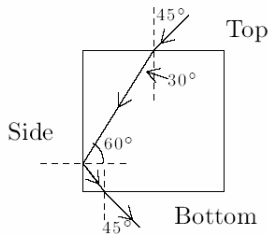


The person must be able to see the top of his head and the bottom of his feet. From the figure it is evident that the mirror height is:

$$h_{\text{mirror}} = h - h_1/2 - h_2/2 = h/2$$

The mirror must be half the height of the person. So for a person of height six ft person, the mirror must be 3 ft high.

2-5. Refer to the figure.



At Top: $(1) \sin 45 = \sqrt{2} \sin \theta' \Rightarrow \theta' = 30$

At Side: $\sqrt{2} \sin 60 = (1) \sin \theta', \sin \theta' = \sqrt{1.5} > 1$

Thus total internal reflection occurs.

At Bottom: reverse of Top: $\theta' = 45^\circ$

2-6. The microscope first focuses on the scratch using direct rays. Then it focuses on the image I_2 formed in a two-step process: (1) reflection from the bottom to produce an intermediate image I_1 and (2) refraction through the top surface to produce an image I_2 . Thus, I_1 is at $2t$ from top surface, and I_2 is at the apparent depth for I_1 , serving as the object: $s' = \frac{2t}{n}$ or $n = \frac{2t}{s'} = \frac{3}{1.87} = 1.60$

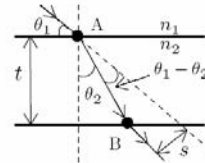
2-8. Referring to the figure one can see that,

$$s = AB \sin(\theta_1 - \theta_2) \text{ and } AB = \frac{t}{\cos \theta_2}. \text{ Therefore,}$$

$$s = \frac{t \sin(\theta_1 - \theta_2)}{\cos \theta_2}. \text{ For } t = 3 \text{ cm, } n_2 = 1.50, \theta_1 = 50^\circ,$$

$$\text{Snell's law gives, } \sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1 = \frac{1}{1.5} \sin 50^\circ.$$

$$\text{Then, } \theta_2 = 30.71^\circ \text{ and } s = \frac{3 \sin(50^\circ - 30.71^\circ)}{\cos 30.71^\circ} = 1.153 \text{ cm.}$$



2-9. Image of near end: $s = 60 \text{ cm, } \frac{1}{60} = \frac{1}{s'} = \frac{1}{-40}, s' = -24 \text{ cm}$

Image of far end: $s = 60 + 100 \text{ cm, } \frac{1}{160} + \frac{1}{s'} = \frac{1}{-40}, s' = -32 \text{ cm. So, } L' = \Delta s' = -24 - (-32) = 8 \text{ cm}$

2-10. (a) See Figure 2-34 in the text. Image due to rays directly from bubble through plane interface:

$$\frac{n_1}{s} + \frac{n_2}{s'} = 0 \text{ or } \frac{1.5}{s} + \frac{1}{s'} = 0 \Rightarrow s' = -3.33 \text{ cm.}$$

(b) Image due to rays first reflected in spherical mirror, then refracted through plane interface:

$$\text{reflection: } \frac{1}{2} + \frac{1}{s_1'} = -\frac{2}{R} \text{ and } \frac{1}{2.5} + \frac{1}{s_1'} = -\frac{2}{-7.5} \quad s_1' = -7.5 \text{ cm}$$

$$\text{refraction: } \frac{n_1}{s} + \frac{n_2}{s_2'} = 0 \text{ or } \frac{1.5}{15} + \frac{1}{s_2'} = 0 \quad s_2' = -10 \text{ cm}$$

Thus the images are at 3.33 cm and 10 cm behind the interface.

2-32. Refer to Figure 2-39 in the text.

(a) Let the angle with the normal to the interface in each region of index of refraction n_i be θ_i . Then applying Snell's law sequentially at each interface leads to,

$$n_0 \sin \theta_0 = n_1 \sin \theta_1 = n_2 \sin \theta_2 \dots = n_i \sin \theta_i \dots = n_f \sin \theta_f$$

That is,

$$n_0 \sin \theta_0 = n_f \sin \theta_f$$

(b) In each medium the lateral displacement is $t_i \tan \theta_i$. The total lateral displacement y due to N media can be written as,

$$y = \sum_{i=1}^n t_i \tan \theta_i$$

where $\sin \theta_i = (n_0/n_i) \sin \theta_0$.

2-34. The focal length is the image position for incident parallel light rays (object at ∞). In all cases the following relation is to be used

$$\frac{n_1}{s} + \frac{n_2}{s'} = \frac{n_2 - n_1}{R} \Rightarrow \frac{n_1}{\infty} + \frac{n_2}{f} = \frac{n_2 - n_1}{R} \Rightarrow \frac{n_2}{f} = \frac{n_2 - n_1}{R}$$

For the situation in which the center of curvature in medium with $n = 4/3$:

For light incident from the medium of index 1: $\frac{4/3}{f} = \frac{4/3 - 1}{10}$ or $f = +40$ cm

For light incident from the medium of index 4/3: $\frac{1}{f} = \frac{1 - 4/3}{-10}$ or $f = +30$ cm

For the situation in which the center of curvature is in the medium with $n = 1$,

For light incident from the medium of index 4/3: $\frac{4/3}{\infty} + \frac{1}{f} = \frac{1 - 4/3}{10}$ or $f = -30$ cm

For light incident from the medium of index 1: $\frac{1}{\infty} + \frac{4/3}{f} = \frac{4/3 - 1}{-10}$ or $f = -40$ cm