

23-19. Given $n_I = 5.3$ at $\lambda = 589.3 \text{ nm}$. (a) $\alpha = 4\pi n_I/\lambda = 4\pi (5.3)/(589.3 \text{ nm}) = 0.113 \text{ nm}^{-1}$

(b) $I = I_0 e^{-\alpha s}$. For $I = 0.01 I_0$, $e^{-\alpha s} = 0.01 \Rightarrow s = (-1/\alpha) \ln(0.01) = 40.75 \text{ nm} = 0.069 \lambda$

23-21. (a) The penetration depth is

$$|z|_{1/e} = \frac{1}{\alpha} = \frac{\lambda}{2\pi} \frac{1}{\sqrt{\sin^2 \theta/n^2 - 1}} = \frac{0.546 \mu\text{m}}{2\pi} \frac{1}{\sqrt{\sin^2(45^\circ)/(1/1.6)^2 - 1}} = 0.164 \mu\text{m}$$

(b) Since irradiance is proportional to the square of the field amplitude and with $\alpha = \frac{1}{|z|_{1/e}} = 6.089 \mu\text{m}^{-1}$,

$$\frac{I}{I_0} = e^{-2\alpha|z|} = e^{-2(6.089 \mu\text{m}^{-1})(1 \mu\text{m})} = 5.1 \times 10^{-6}$$

25-1. (a) Consider,

$$K \equiv n^2 = (n_R + i n_I)^2 = n_R^2 - n_I^2 + 2i n_I n_R = K_R + i K_I$$

$$K_R = n_R^2 - n_I^2, K_I = 2 n_I n_R$$

Solving these two relations for n_R and n_I proceeds as,

$$K_I = 2 n_I n_R = 2 n_I \sqrt{K_R^2 + n_I^2}$$

$$K_I^2 = 4 n_I^2 (K_R^2 + n_I^2)$$

$$4 n_I^4 + 4 K_R^2 n_I^2 - K_I^2 = 0$$

$$n_I^2 = \frac{-4 K_R \pm \sqrt{16 K_R^2 + 16 K_I^2}}{8} = \frac{-K_R \pm \sqrt{K_R^2 + K_I^2}}{2}$$

To make $n_I^2 > 0$, choose the + sign. Thus,

$$n_I = \left[\frac{-K_R + \sqrt{K_R^2 + K_I^2}}{2} \right]^{1/2}$$

$$n_R^2 = K_R + n_I^2 = \frac{2 K_R}{2} + \frac{-K_R + \sqrt{K_R^2 + K_I^2}}{2} = \frac{K_R + \sqrt{K_R^2 + K_I^2}}{2}$$

$$n_R = \left[\frac{K_R + \sqrt{K_R^2 + K_I^2}}{2} \right]^{1/2}$$

(b) If $K_I \approx K_R$,

$$n_R = \left[\frac{K_I + \sqrt{2 K_I^2}}{2} \right]^{1/2} = \sqrt{K_I} \left(\frac{1 + \sqrt{2}}{2} \right)^{1/2} = 1.099 \sqrt{K_I}$$

$$n_I = \left[\frac{-K_I + \sqrt{2 K_I^2}}{2} \right]^{1/2} = \sqrt{K_I} \left(\frac{-1 + \sqrt{2}}{2} \right)^{1/2} = 0.455 \sqrt{K_I}$$

25-7. (a) $\delta_{A1} = \left(\frac{2}{\sigma \mu_0 \omega} \right)^{1/2} = \left(\frac{2}{3.54 \times 10^7 (4\pi \times 10^{-7}) 2\pi \times 6 \times 10^4} \right)^{1/2} \text{ m} = 0.345 \text{ mm}$

(b) $\delta_{s.w.} = \left(\frac{3.54 \times 10^7}{4.3} \right) \times \delta_{A1} = 0.991 \text{ m} \approx 1 \text{ m}$

25-8. $\delta_{Ag} = \left(\frac{\lambda}{\sigma \mu_0 \pi c} \right)^{1/2} = \left(\frac{0.1}{3 \times 10^7 (4\pi \times 10^{-7}) \pi (3 \times 10^8)} \right)^{1/2} \text{ m} = 1.68 \times 10^{-6} \text{ m} = 1.68 \mu\text{m}$

As long as the silver coating is thicker than this the silver-plated brass component would work.

25-9. (a) $I = I_0 e^{-\alpha x} \Rightarrow (I/I_0) = (1/4) = e^{-\alpha x} = e^{-\alpha(3.42\text{m})} \Rightarrow 3.42 \alpha = \ln(4) \Rightarrow \alpha = 0.405 \text{ m}^{-1}$

(b) $(I/I_0) = (1/100) = e^{-(0.405\text{m}^{-1})x} \Rightarrow (0.405 \text{ m}^{-1})x = \ln(100) \Rightarrow x = 11.37 \text{ m}$