Physics 9C-C Midterm Exam #1

(Winter of 2021)

1. Point charges

In the figure below, a point charge $q_1 = +1$ nC and another charge $q_2 = -1$ nC are placed on the x-axis and separated by 8 cm. Let Point A in the middle be the origin. A target charge Q = + 2 nC is placed on the y-axis at y = + 3 cm (Point B). $\varepsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2$.

- (a) (**10 points**) Find the x- and y-components of the net Coulomb force on Q (at Point B) exerted by q₁ and q₂.
- (b) (8 points) Find the electric potential difference, $V_A V_B$, produced by the electric fields of q_1 and q_2 .
- (c) (8 points) When Q is moved from Point C to Point D, what is the potential energy change for Q, i.e., $U_C(Q) U_D(Q)$, in the electric field produced by q_1 and q_2 ?



2. Effect of a combination of large charge sheets

In the following figure, two infinitely large charge sheets, parallel to each other, are separated by a distance d. One has a surface charge density σ and the other has a surface charge density twice as large. Let the x-axis be perpendicular to the sheets. Point B is in the middle between the two sheets.



- (a) (12 points) Find the electric fields at A, B, and C.
- (b) (15 points) Find the electric potential difference between A and C.

3. Combination of differently shaped charge distributions:

In the figure below, a long insulating cylindrical shell with radius R and negligible thickness carries a uniformly distributed charge λ per unit length. It is place between two infinitely large insulating charge sheets. The charge sheets and the cylindrical axis of the shell are parallel.

- (a) (10 points) Find the electric field at B
- (b) (10 points) Find the potential difference between the center of the cylindrical shell A and Point B, i.e., $V_A V_B$.
- (c) (5 points) Find the electric potential difference between Point C and D, i.e., $V_C V_D$.



4. Effect of two spherically symmetric charge distributions

In the figure below, an insulating solid sphere with radius R is uniformly charged throughout its volume with + Q. An insulating spherical shell with radius R and negligible thickness is uniformly charged with - Q. The distance between centers of the two charge distributions is 3R. Point A is half way between the center and the surface of the solid sphere. Point B is half way between the center and the surface of the thin shell.



- (a) (8 points) Find the total electric field at A;
- (b) (6 points) Find the total electric field at B;
- (c) (10 points) Find the electric potential difference, $V_A V_B$, produced by just the charge on the solid sphere;
- (d) (8 points) Find the electric potential difference, $V_A V_B$., produced by just the charge on the thin spherical shell.